

2.3 Set Operations

M. Goodroe - Quantitative Skills and Reasoning

Key Terms:

- Union
- Intersection
- Complement
- Difference
- DeMorgan's Laws
- Inclusion/Exclusion Principle

Name: _____

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Let $U = \{q, r, s, t, u, v, w, x, y, z\}$

$A = \{q, s, u, w, y\}$

$B = \{q, s, y, z\}$

$C = \{v, w, x, y, z\}$. List the elements in the set.

1) $A \cap B'$

2) $(A \cap B)'$

3) $C' \cup A'$

4) $A - C$

Describe the indicated set in words and find the set.

5) $P - (E \cup C)'$, given the following information:

The table gives features of different dishwasher

model	price (dollars)	clean china	clean glassware	energy efficiency	water usage
a	712	excellent	good	good	low
b	455	excellent	good	fair	medium
c	554	excellent	good	good	high
d	606	excellent	good	good	high
e	556	good	fair	good	low
f	385	excellent	fair	good	medium
g	480	good	fair	fair	medium
h	361	good	fair	fair	medium
i	263	fair	poor	good	medium

In the universal set $U = \{a, b, c, \dots, i\}$, let the following characteristics be defined:

P = price is at or below \$455

C = does an excellent job of cleaning china

G = does an excellent job of cleaning glassware

E = has a good energy efficiency rating

F = has low water usage

6) $(P \cup L) - (S \cap C)$, given the following information:
The table gives the approximate nutritional value per serving of foods at a certain restaurant.

food	calories	protein (grams)	fat (grams)
Chow Mein	240	23	16
Pizza (cheese)	120	15	9
Bean Burrito	340	20	4
Linguini & Meatballs	330	19	13
Pea Soup	250	7	7
Chicken Salad	210	33	8
Ice Cream	270	3	13

Let:

$C = \{m : m \text{ provides } 251 \text{ or more calories}\}$

$P = \{m : m \text{ provides } 20 \text{ or more grams of protein}\}$

$F = \{m : m \text{ provides } 10 \text{ or more grams of fat}\}$

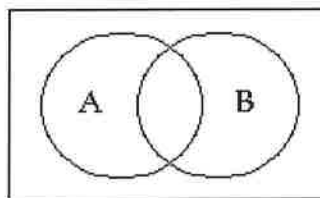
$L = \{m : m \text{ provides } 150 \text{ or more mg of calcium}\}$

$S = \{m : m \text{ provides } 1000 \text{ or more mg of sodium}\}$

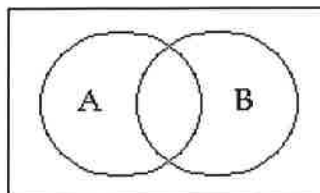
$A = \{m : m \text{ provides } 1000 \text{ or more A.U. of Vitamin A}\}$

Shade the Venn diagram to represent the set.

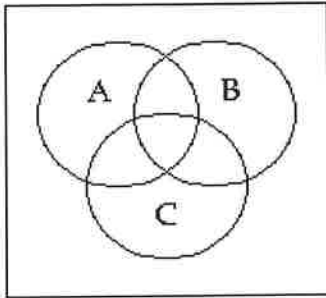
7) $A' \cap B'$



8) $(A \cup B) \cap (A \cap B)'$



9) $(A \cap B \cap C)'$



15) $n((C \cup B) - (A \cup B))$

Let A and B be sets with cardinal numbers, $n(A) = a$ and $n(B) = b$, respectively. Decide whether the statement is true or false.

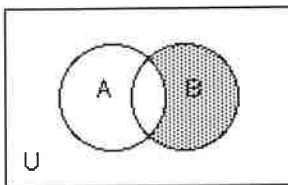
16) $B \subset (B \cap A)$

17) If $B \subset A$, $n(B) = n(A - B)$.

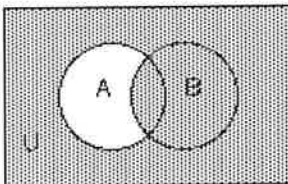
18) If $B \subset A$, $n(B) = n(A) - n(A - B)$.

Write a description of the shaded region using the symbols A, B, C, \cup , \cap , $-$, and $'$ as needed.

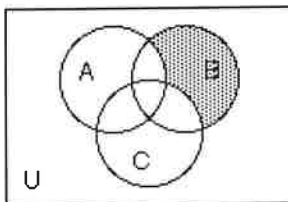
10)



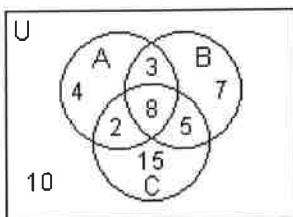
11)



12)



Use the Venn diagram below to find the number of elements in the region.



13) $n(A)$

14) $n(C - A)$