2.2 Comparing Sets

M. Goodroe - Quantitative Skills and Reasoning

Objectives:

- 1. Determine when sets are equal
- 2. Distinguish between the ideas of "equal" and "equivalent" sets.
- 3. Explain the difference between subsets and proper subsets
- 4. Use Venn diagrams to illustrate set relationships.
- 5. Determine the number of subsets of a given set.

Key Terms:

Equal Sets
Equivalent Sets
One-to-One Corresspondence
Subset
Proper Subset
Venn Diagram

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Decide whether the sets are equal.

- 1) {parsley, thyme, saffron, oregano} and {y : y is an herb}
- 2) $\{y: y \text{ was an American President in the year 1573} \}$ and \emptyset

Decide whether the statement is true or false.

- 3) $\emptyset \subseteq \{4, 8, 12, 16, 20\}$
- 4) $\{12, 84, 145, 264\} \subseteq \{12, 24, 36, ..., 1080\}$

Decide whether the sets are equivalent.

- 5) {d: d is a month of the year} and {g: g is a state in the United States}
- 6) {x : x is a multiple of 10 between 1 and 100, inclusive} and {9, 18, 27, ..., 90}

List the subsets.

- List all of the two element subsets of the set {a, b, c, d}.
- 8) List all of the three element subsets of the set {a, b, c, d, e}.

Name:

Use the following definitions to determine if the statement is true or false.

 $N = \{x : x \text{ is a natural number}\}\$

 $I = \{x : x \text{ is an integer}\}\$

 $R = \{x : x \text{ is a real number}\}\$

 $W = \{x : x \text{ is a whole number}\}\$

 $Q = \{x : x \text{ is a rational number}\}\$

- 9) W is a subset of W, I, Q, and R.
- 10) W is a subset of N, W, I, Q, and R.
- 11) I is a proper subset of Q and R.
- 12) I is a proper subset of N, W, Q, and R.

Find the number of subsets of the set.

- 13) {14, 15, 16}
- 14) {math, English, history, science, art}
- 15) $\{x \mid x \text{ is a day of the week}\}$