

$$40/40 = 100$$

Foundations for College Algebra
University of North Georgia
Fall 2016
Quiz # 8

- Extra Credit: 18 pts
- 58/40 = 145 possible

Factor the following completely.

1. $x^2 - 16x + 48$ $ac = 48$ $b = -16$ $\begin{array}{c|c} - & - \\ \hline 12 & 4 \end{array}$

$$x^2 - 12x - 4x + 48$$
$$x(x-12) - 4(x-12)$$
$$\boxed{(x-12)(x-4)}$$

Check

$$(x-12)(x-4)$$
$$x^2 - 4x - 12x + 48$$
$$x^2 - 16x + 48 \checkmark$$

2. $x^2 - 4x - 5$ $ac = -5$ $b = -4$ $\begin{array}{c|c} - & + \\ \hline 5 & 1 \end{array}$

$$x^2 - 5x + x - 5$$
$$x(x-5) + 1(x-5)$$
$$\boxed{(x-5)(x+1)}$$

$$(x-5)(x+1)$$
$$x^2 + x - 5x - 5$$
$$x^2 - 4x - 5 \checkmark$$

3. $6x^2 + 17x + 7$ $ac = 42$ $b = 17$ $\begin{array}{c|c} + & + \\ \hline 14 & 3 \end{array}$

$$6x^2 + 14x + 3x + 7$$
$$2x(3x+7) + 1(3x+7)$$
$$\boxed{(3x+7)(2x+1)}$$

$$(3x+7)(2x+1)$$
$$6x^2 + 3x + 14x + 7$$
$$6x^2 + 17x + 7 \checkmark$$

4. $25x^2 - 4$ $a = 5x$ $b = 2$

$$(5x+2)(5x-2)$$

$$(5x+2)(5x-2)$$
$$25x^2 - 10x + 10x - 4$$
$$25x^2 - 4 \checkmark$$

5. $27x^3 + 8$ $a = 3x$ $b = 2$

$$(3x+2)(9x^2 - 6x + 4)$$

$$(3x+2)(9x^2 - 6x + 4)$$
$$27x^3 - 18x^2 + 12x + 18x^2 - 12x + 8$$
$$27x^3 + 8 \checkmark$$

Solve each equation using factoring.

6. $x^2 = -7x + 30$

$$x^2 + 7x - 30 = 0 \quad ac = -30 \quad \begin{array}{l} + \\ - \\ \hline 10 \quad 3 \end{array}$$

$$x^2 + 10x - 3x - 30 = 0 \quad b = 7$$

$$x(x+10) - 3(x+10) \quad \textcircled{1} \quad x+10=0$$

$$(x+10)(x-3) \quad \boxed{x = -10}$$

7. $60 - x^2 = 11x$

$$0 = x^2 + 11x - 60 \quad ac = -60$$

$$0 = x^2 + 15x - 4x - 60 \quad b = 11 \quad \begin{array}{l} + \\ - \\ \hline 15 \quad 4 \end{array}$$

$$0 = x(x+15) - 4(x+15) \quad \textcircled{1} \quad x+15=0$$

$$0 = (x+15)(x-4) \quad \boxed{x = -15}$$

8. $x^2 - 1 = 0 \quad a = 1 \quad b = 1$

$$(x+1)(x-1) = 0 \quad \textcircled{2} \quad x-1=0$$

$$x = \pm 1 \quad \boxed{x = 1}$$

$$(-10)^2 = -7(-10) + 30$$

$$100 = 70 + 30 \quad \checkmark$$

$$(3)^2 = -7(3) + 30$$

$$9 = -21 + 30 \quad \checkmark$$

$$60 - (-15)^2 = 11(-15)$$

$$60 - 225 = -165$$

$$-165 = -165 \quad \checkmark$$

$$60 - (4)^2 = 11(4)$$

$$60 - 16 = 44$$

$$44 = 44 \quad \checkmark$$

$$(1)^2 - 1 = 0$$

$$1 - 1 = 0 \quad \checkmark$$

$$(-1)^2 - 1 = 0$$

$$1 - 1 = 0 \quad \checkmark$$

9. State the Zero Product Property.

$$a \cdot b = 0$$

10. Show that $(x - 4)(x - 21) = x^2 - 25x + 84$

$$x^2 - 21x - 4x + 84$$

$$x^2 - 25x + 84 \quad \checkmark$$

$$x^2 - 25x + 84 \quad ac = 84$$

$$x^2 - 21x - 4x + 84 \quad b = -25$$

$$x(x-21) - 4(x-21) \quad \begin{array}{l} - \\ + \\ \hline 21 \quad 4 \end{array}$$

$$(x-21)(x-4) \quad \checkmark$$

BONUS (5 points) Factor the following completely.

$$14x^2 + 11x - 15 \quad ac = -210$$

$$14x^2 + 21x - 10x - 15 \quad b = 11 \quad \begin{array}{l} + \\ - \\ \hline 15 \quad 4 \end{array} \quad \begin{array}{l} p \\ q \\ \hline -210 \\ 11 \end{array}$$

$$7x(2x+3) - 5(2x+3)$$

$$\boxed{(2x+3)(7x-5)}$$

16	5	-80	✓
18	7	-126	✓
22	11	-242	✓
21	10	-210	✓

$$(2x+3)(7x-5)$$

$$14x^2 - 10x + 21x - 15$$

$$14x^2 + 11x - 15 \quad \checkmark$$